# Geothermics and Geothermal Energy Deep Open Geothermal Systems

## Stefan Hergarten

Institut für Geo- und Umweltnaturwissenschaften Albert-Ludwigs-Universität Freiburg





#### Steps of Conversion

Thermal energy  $\rightarrow$  mechanical work: turbine; rather low efficiency due to thermodynamic limitation

Mechanical work  $\rightarrow$  electricity: generator; high efficiency

## Converting Geothermal Energy to Electricity



#### The Thermodynamic Limitation (Carnot Cycle)

$$\delta S = \frac{\delta Q_h}{T_h} + \frac{\delta Q_c}{T_c} \ge 0 \tag{1}$$

#### where

- $\delta {\it Q}_{\it h}~=~$  thermal energy supplied to to the hot system
  - < 0 (from the geothermal reservoir into the turbine)
  - $T_h$  = temperature of the hot system
- $\delta Q_c$  = thermal energy supplied to the cold system
  - > 0 (out of the turbine)
  - $T_c$  = temperature of the cold system



#### The Thermodynamic Limitation (Carnot Cycle)

Mechanical work yielded by one cycle (conservation of energy):

$$\delta W = -\left(\delta Q_h + \delta Q_c\right) \leq -\delta Q_h \left(1 - \frac{T_c}{T_h}\right) = -\eta_{\max} \delta Q_h \quad (2)$$

with the maximum efficiency

$$\eta_{\max} = \frac{T_h - T_c}{T_h} \tag{3}$$

Consequence for the electrical, mechanical and thermal power of a geothermal power plant:

$$P_{
m el}~<~P_{
m me}~<~\eta_{
m max}\,P_{
m th}$$

## Converting Geothermal Energy to Electricity



#### Maximum Efficiency of Converting Thermal Energy



## Main Types of Geothermal Power Plants



#### General Principle: Clausius-Rankine Cycle





## Main Types of Geothermal Power Plants

## FREBURG

#### Dry Steam Power Plants



Source: Office of Energy Efficiency and Renewable Energy



#### Dry Steam Power Plants

- Rather simple technology
- First geothermal production of electricity: Larderello 1904
- $\bullet\,$  Biggest geothermal power plant on Earth: "The Geysers", California, USA, 750  $\rm MW_{el}$
- Limited to few locations on Earth

## Main Types of Geothermal Power Plants

# FREBURG

#### Flash Steam Power Plants



Source: Office of Energy Efficiency and Renewable Energy



#### Flash Steam Power Plants

- Most common type of geothermal power generation plants in operation today
- Reasonable efficiency only for high-enthalpy resources (  $T > 200^{\circ}$ C)

## Main Types of Geothermal Power Plants



#### Binary Cycle Power Plants



Source: Office of Energy Efficiency and Renewable Energy



#### Binary Cycle Power Plants

- Heat transfer to a fluid with a boiling point below 100°C by a heat exchanger
- Applicable to low-enthalpy resources (  $T < 200^{\circ}$ C)
- Expensive technology
- Types:

Organic Rankine Cycle (ORC): Transfer heat to an organic fluid with a low boiling point and operate the turbine with this fluid, e.g., n-perfluorpentane ( $C_5F_{12}$ , boiling point 30°C,  $T_c \approx 75^{\circ}$ C) Kalina cycle: Ammonia solution where the concentration of ammonia varies during the cycle; power plants in Germany at Unterhaching and Bruchsal



#### ORC Power Plants in Germany

Location	Depth [m]	T [°C]	$Q\left[\frac{1}{s}\right]$	$P_{\rm th}$ [MW]	$P_{\rm el}$ [MW]
Dürrnhaar	4114	130	135		5.5
Grünwald	4083	130 150		50	4.5
Insheim	3650	165 85			4.8
Kirchstockach	3750	139	145		5.5
Landau	3340	155	70		3.8
Neustadt-Glewe	2455	99	35	5.5	0.23
Sauerlach	4480	143	110		4.0
Simbach/Braunau	1942	80	74	7	0.2
Traunreut	4500	118	130		5.0(?)



#### Kalina Cycle Power Plants in Germany

Location	Depth [m]	T [°C]	$Q\left[\frac{1}{s}\right]$	$P_{\rm th}$ [MW]	P <sub>el</sub> [MW]
Unterhaching	3350	122	150	38	3.36*
Bruchsal	2542	120	24	5.5	0.55

\* until 2017

#### Principle

- Hot water is extracted at one or more wells.
- Cold water is (re)injected at another well; in most cases at the same rate as total extraction.
- Flow of water through a porous rock.



Source: Borehole Wireline

#### Major Problem

Maintaining the fluid circulation in the rock consumes a considerable part of the produced energy.  $$_{15/}$$ 



#### Porosity of Rocks

Total porosity:  $\phi = \frac{\text{void volume}}{\text{total volume}}$ ;  $0 \le \phi < 1$ ; often measured in percent Effective porosity: only accessible pores and volume of water that can be extracted

Typical porosity values:

	$\phi_{\sf tot}$ [%]	$\phi_{\rm eff}$ [%]
equally sized spheres	26–48	26–48
soil	55	40
clay	50	2
sand	25	22
limestone	20	18
sandstone (semiconsolidated)	11	6
granite	0.1	0.09

Source: GlobalSecurity.org

## Fundamentals - Fluid Flow in Porous Media

# FREBURG

(5)

#### Darcy's Law

- Empirically found by Henry Darcy (1856).
- Describes the average flow through a porous medium on macroscopic scales.
- Simplest form (without gravity):

$$ec{v}(ec{x},t) = -rac{k}{\eta} 
abla p(ec{x},t)$$

where

- $\vec{v}$  = volumetric flow rate (Darcy velocity)  $\left[\frac{m}{s}\right]$
- p = fluid pressure [Pa]
- k = hydraulic permeability [m<sup>2</sup>]
- $\eta = dynamic viscosity of the fluid [Pas]$
- Basically the same as Fourier's law of heat conduction.



#### The Hydraulic Permeability

• Units:

SI unit: m<sup>2</sup> Widely used unit: Darcy (D)

$$1 \text{ D} = 9.869 \times 10^{-13} \text{ m}^2 \approx 10^{-12} \text{ m}^2 = 1 \, \mu \text{m}^2$$

- k = 1 D results in a flow rate of  $1 \frac{\text{cm}}{\text{s}}$  at a pressure drop of  $1 \frac{\text{atm}}{\text{cm}}$  in water at 20°C ( $\eta = 10^{-3} \text{ Pas}$ ).
- Typical values:

Medium	<i>k</i> [D]	Medium	<i>k</i> [D]
gravel	10-1000	limestone	$10^{-6} - 100$
sand	0.01-10	fractured igneous rocks	$10^{-6} - 10$
silt	$10^{-3} - 0.1$	unfractured igneous rocks	$10^{-9} - 10^{-6}$



(6)

#### The Darcy Equation

Balance equation for the mass of water per bulk volume

$$\frac{\partial \chi}{\partial t} = -\operatorname{div}\left(\rho_f \vec{v}\right) = \operatorname{div}\left(\rho_f \frac{k}{\eta} \nabla p\right)$$

where



#### The Darcy Equationi Compared to the Heat Conduction Equation

Basically the same equation as the heat conduction equation with a different meaning of the parameters.

heat conduction	Т	$\lambda$	ho c	$\kappa = \frac{\lambda}{ ho c}$
Darcy flow	р	$\rho_f \frac{k}{\eta}$	S	$\tilde{\kappa} = rac{ ho_f k}{\eta S}$

If all parameters are constant:

$$\frac{\partial T}{\partial t} = \kappa \Delta T, \qquad \vec{q} = -\lambda \nabla T$$
(8)
$$\frac{\partial p}{\partial t} = \tilde{\kappa} \Delta p, \qquad \vec{v} = -\frac{k}{\eta} \nabla p$$
(9)



#### Superposition of Solutions

The simplest form of Darcy's equation is linear.

Solutions can be superposed:

$$p(\vec{x}, t) = p_0(\vec{x}) + p_1(\vec{x}, t) + p_2(\vec{x}, t) + \dots$$
(10)  
$$\vec{v}(\vec{x}, t) = \vec{v}_0(\vec{x}) + \vec{v}_1(\vec{x}, t) + \vec{v}_2(\vec{x}, t) + \dots$$
(11)

where

 $p_0, \vec{v}_0 =$  natural pressure and Darcy velocity without wells  $p_i, \vec{v}_i =$  additional pressure and Darcy velocity caused by well #i



#### The Simplest Model for a Hydrothermal Well



Vertical borehole in an aquifer of a thickness *I* Simplifications:

- All parameters (k, S,  $\rho_f$ ,  $\eta$ ) constant
- Only horizontal flow in radial direction

Basically the same solution as for the temperature drop of a downhole heat exchanger

Use variables p and  $\vec{v}$  for the additional pressure and Darcy velocity instead instead of  $p_i$  and  $\vec{v}_i$ .



#### The Simplest Model for a Hydrothermal Well

Downhole heat exchanger:

$$T(r,t) = -\frac{P_l}{4\pi\lambda} E_1\left(\frac{r^2}{4\kappa t}\right)$$
(12)

Hydrothermal well:

$$p(r,t) = \frac{\frac{\rho_f Q}{l}}{4\pi\rho_f \frac{k}{\eta}} E_1\left(\frac{r^2}{4\tilde{\kappa}t}\right) = \frac{\eta Q}{4\pi k l} E_1\left(\frac{r^2}{4\tilde{\kappa}t}\right)$$
(13)

where

$$Q$$
 = rate of injection  $\left[\frac{m^3}{s}\right]$ ,  $Q < 0$  for extraction

#### Well Doublets

 $\tilde{\kappa} \gtrsim 1 \frac{\text{m}^2}{\text{s}}$  for highly permeable rocks ( $k \gtrsim 0.01 \text{ D}$ ) required for hydrothermal systems if the rock is fully saturated with water.

Pressure rapidly decreases around an extraction well.

Solution: Use a well doublet consisting of an injection well and an extraction well working at the same flow rate.

$$p(x, y, t) = \frac{\eta Q}{4\pi k l} \left( E_1 \left( \frac{r_i^2}{4\tilde{\kappa}t} \right) - E_1 \left( \frac{r_e^2}{4\tilde{\kappa}t} \right) \right)$$
(14)

where  $r_{i/e}$  is the distance of the considered point from the injection / extraction well.





#### Pressure Distribution of a Well Doublet Compared to a Single Well





#### Well Doublets

Use the approximation

$$E_1(v) \approx -\ln(v) - 0.5772 \quad \text{for} \quad v \ll 1$$
 (15)

$$\begin{aligned}
\Psi \\
p(x, y, t) \approx \frac{\eta Q}{4\pi k l} \left( -\ln\left(\frac{r_i^2}{4\tilde{\kappa}t}\right) + \ln\left(\frac{r_e^2}{4\tilde{\kappa}t}\right) \right) & (16) \\
&= \frac{\eta Q}{2\pi k l} \ln\frac{r_e}{r_i} & (17)
\end{aligned}$$

is independent of t (steady-state flow conditions).



#### Pressure and Flow Lines of a Simple Well Doublet





#### The Simplest Model for a Well Doublet

Limitation: In principle only valid

- for confined aquifers or
- if the horizontal distance of the wells is much smaller than the open borehole length /

Mechanical power required for maintaining the flow:

$$P = (p_i - p_e) Q \tag{18}$$

where

 $p_i$  = pressure at the walls of the injection well  $p_e$  = pressure at the walls of the extraction well



#### Well Triplet



## Enhanced Geothermal Systems



#### Hydraulic Fracturing for Increasing the Permeability













#### Drill a well to explore

Inject water to cause slip on faults (high water pressure pushes fractures open)

Injection extends a network of connected fractures

Inject water to sweep heat to a production well

Maximize production rate and lifetime

Source: NewEnergyNews



### Environmental Issues related to Hydraulic Fracturing

- Large amounts of contaminated water if fracturing is supported by additional chemicals
- Fluid-induced seismicity

## Heat Transport in Geothermal Systems



#### Mechanisms of Heat Transport in Porous Media

Solid matrix: conduction

Fluid: conduction and advection

### Heat Exchange Between Fluid and Matrix

Length scale of heat conduction:

$$L(t) = \sqrt{\kappa t}$$

Water: 
$$\kappa = 1.4 \times 10^{-7} \frac{\text{m}}{\text{s}}$$
  
Rocks:  $\kappa \approx 10^{-6} \frac{\text{m}^2}{\text{s}}$ 

Fluid and matrix rapidly adjust to the same temperature locally.

(19)



#### The Heat Equation for a Fluid

Heat flux density for a fluid moving at a velocity  $\vec{v}$ :





24

#### The Heat Equation for a Porous Medium

$$(\rho_m c_m + \phi \rho_f c_f) \frac{\partial T}{\partial t} = \operatorname{div} \left( (\lambda_m + \phi \lambda_f) \nabla T - \rho_f c_f T \vec{v} \right) \quad (23)$$

where

 $\rho_f, c_f, \lambda_f = \text{parameters of the fluid}$   $\rho_m, c_m, \lambda_m = \text{parameters of the dry matrix (not the solid!)}$   $\phi = \text{porosity}$   $\vec{v} = \text{Darcy velocity}$ 

Effective velocity of heat advection:

$$ec{v}_{a} = rac{
ho_{f}c_{f}}{
ho_{m}c_{m}+\phi
ho_{f}c_{f}} ec{v} pprox 1.7 ec{v}$$



(25)

#### Velocities of Fluid Flow and Heat Transport

Mean interstitial velocity of the water particles

$$p = \frac{\vec{v}}{\phi}$$

is significantly higher than the flow rate (Darcy velocity)  $\vec{v}$ . Effective velocity of heat advection

 $\vec{v}$ 

$$\vec{v}_a = \frac{\rho_f c_f}{\rho_m c_m + \phi \rho_f c_f} \vec{v} \approx 1.7 \vec{v}$$
(26)

is also higher than the flow rate  $\vec{v}$ , but lower than the mean interstitial velocity  $\vec{v}_p$ .

## Heat Transport in Geothermal Systems



(27)

(28)

#### Velocities of Fluid Flow and Heat Transport

$$\vec{v}_a = rac{\phi 
ho_f c_f}{
ho_m c_m + \phi 
ho_f c_f} \vec{v}_p = rac{\vec{v}_p}{R}$$

where

$$R = \frac{\rho_m c_m + \phi \rho_f c_f}{\phi \rho_f c_f} = 1 + \frac{\rho_m c_m}{\phi \rho_f c_f}$$

is the coefficient of retardation.

Water circulates R times between the wells until the cold temperature front breaks through (if heat conduction is neglected).